

4558

$$\alpha) \Delta = (\lambda^2 + 1)^2 - 4\lambda^2 = (\lambda^2 + 1 - 2\lambda)(\lambda^2 + 1 + 2\lambda) \\ = (\lambda - 1)^2 \cdot (\lambda + 1)^2 \geq 0$$

$$\begin{cases} P = \frac{\lambda}{\lambda} = 1 > 0 \\ S = \frac{\lambda^2 + 1}{\lambda} > 0 \end{cases} \left. \begin{array}{l} \\ \end{array} \right\} \text{θετικές ρίζες}$$

$$\beta) \text{(i)} E = x_1 \cdot x_2 = \text{[crossed out]} = 1$$

$$\text{(ii)} \Pi = 2 \frac{\lambda^2 + 1}{\lambda} \quad \text{AND} \quad 2 \frac{\lambda^2 + 1}{\lambda} \geq 4$$

$$\Rightarrow \lambda^2 + 1 \geq 2\lambda \Rightarrow (\lambda - 1)^2 \geq 0 \text{ OK}.$$

$$\text{(iii)} \Pi_{\min} \text{ για } \lambda = 1$$

$$f(x) = x^2 - 2x + 1 \Leftrightarrow f(x) = (x - 1)^2$$

$$x_1 = x_2 = 1 \Rightarrow \text{Τετραγωνο}$$