

Θέμα Α

(1)

A1 | γ

A5 |

A2 | δ

α) Σ

β) Λ

A3 | γ

δ) Σ

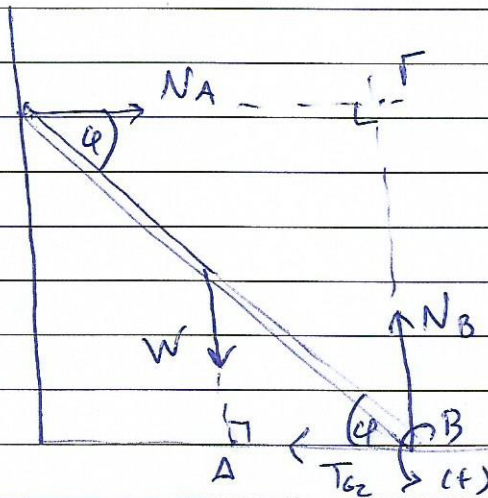
ε) Σ

A4 | β

ε) Λ

Θέμα Β

B1



$$\sum \tau = 0 \Rightarrow W(BA) - N_A(BT) = 0 \Rightarrow W \frac{L}{2} \cos \varphi = N_A L \sin \varphi$$

$$\Rightarrow N_A = \frac{W}{2 \tan \varphi}$$

~~$$\sum F_x = 0 \Rightarrow T_{62} = N_A$$~~

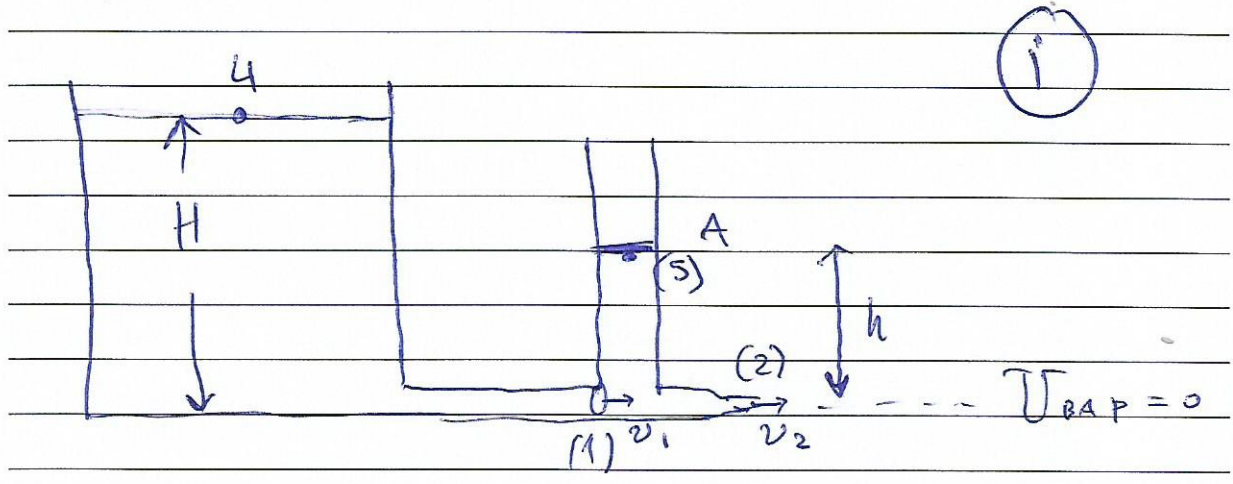
$$\sum F_x = 0 \Rightarrow T_{02} = N_A \Rightarrow T_{02} = \frac{W}{2 \epsilon \varphi \varphi}$$

$$\sum F_y = 0 \Rightarrow N_B = W$$

Πρίνα  $T_{02} \leq \mu \cdot N_B \Rightarrow \frac{W}{2 \epsilon \varphi \varphi} \leq \mu \cdot W \Rightarrow$

$$\Rightarrow \epsilon \varphi \varphi \geq \frac{1}{2\mu} \text{ άρα } (\epsilon \varphi \varphi)_{\min} = \frac{1}{2\mu}$$

B2]



$$h = H/4 \quad A_2 = \frac{A_1}{2}$$

Βερνούλλι  $4 \rightarrow 2$ :  $P_{atf} + \rho g H + \frac{1}{2} \rho v_1^2 = P_{atf} + \frac{1}{2} \rho v_2^2 + 0$

$$\Rightarrow v_2 = \sqrt{2gH}$$

Εξίσωση συνέχειας  $1 \rightarrow 2$

$$A_1 \cdot v_1 = A_2 \cdot v_2 \Rightarrow v_1 = \frac{\sqrt{2gH}}{2}$$

Bernoulli 1 → 2

$$P_1 + \frac{1}{2} \rho v_1^2 = P_{\alpha\alpha\tau} + \frac{1}{2} \rho v_2^2 \Rightarrow$$

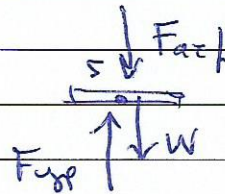
$$\Rightarrow P_1 - P_{\alpha\alpha\tau} = \frac{1}{2} \rho (v_2^2 - v_1^2)$$

$$P_1 - P_{\alpha\alpha\tau} = \frac{1}{2} \rho (4v_1^2 - v_1^2)$$

$$P_1 - P_{\alpha\alpha\tau} = \frac{3}{2} \rho v_1^2 \Rightarrow P_1 - P_{\alpha\alpha\tau} = \frac{3}{2} \rho \cdot \frac{2gH}{4}$$

$$P_1 - P_{\alpha\alpha\tau} = \frac{3}{4} \rho g H \quad (1)$$

Ισορροπία εμβόλου



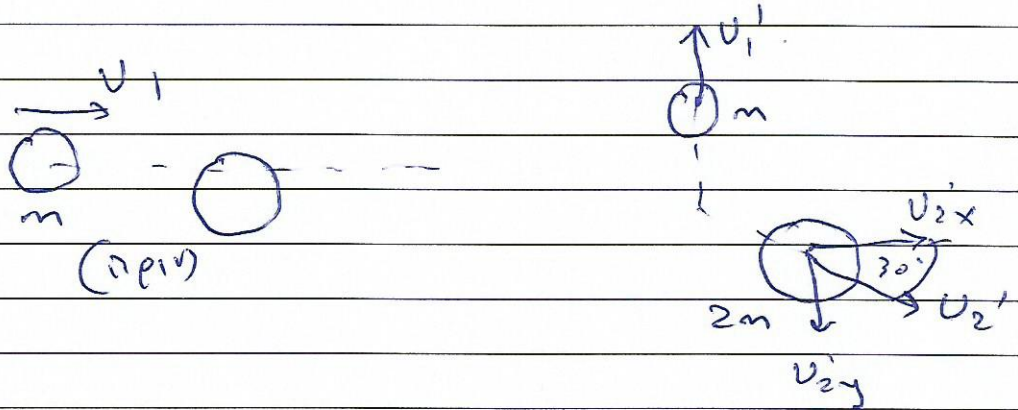
$$F_{\alpha\alpha\tau} = F_{\alpha\alpha\tau} + W \Rightarrow P_5 = P_{\alpha\alpha\tau} + \frac{W}{A} \quad (2)$$

$$P_1 - P_5 = \rho g h \Rightarrow P_1 = P_{\alpha\alpha\tau} + \frac{W}{A} + \rho g \frac{H}{4} \quad (3)$$

$$1, 3 \rightarrow \frac{W}{A} + \rho g \frac{H}{4} = \frac{3}{4} \rho g H$$

$$\frac{W}{A} = \frac{\rho g H}{2} \Rightarrow \boxed{W = \frac{\rho g H A}{2}}$$

B3



$m_1 = m$

$m_2 = 2m$

$m_3 = m$

Α.Δ.Ο στον x'x

$$m \cdot v_1 = 2m \cdot v_2' \cdot \cos 30^\circ \Rightarrow m \cdot v_1 = 2m \cdot v_2' \cdot \frac{\sqrt{3}}{2}$$

$$\Rightarrow \boxed{v_1 = \sqrt{3} \cdot v_2'}$$

Α.Δ.Ο στον y'y:  $0 = m \cdot v_1' - 2m \cdot v_2' \cdot \sin 30^\circ \Rightarrow$

$$\Rightarrow v_1' = 2 \cdot v_2' \cdot \frac{1}{2} \Rightarrow v_1' = v_2'$$

άρα  $v_1 = \sqrt{3} \cdot v_1' \Rightarrow v_1' = \frac{\sqrt{3}}{3} v_1$

Α.Δ.Ο στην οριζόντια:  $m_1 \cdot v_1' = (m_1 + m_3) \cdot v_2$

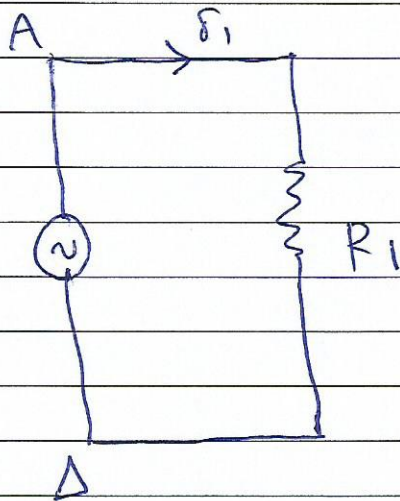
$$\Rightarrow v_2 = \frac{v_1'}{2} = \frac{\sqrt{3}}{6} v_1$$

$$\frac{K_{εγε}}{K_i} = \frac{\frac{1}{2} \cdot 2m \cdot \left(\frac{\sqrt{3}}{6} v_1\right)^2}{\frac{1}{2} m v_1^2} = \frac{1}{6} \quad \text{iii'}$$

Πρόβλημα Γ

$$v = V \cdot \mu(500\pi t) \text{ (S.I)}$$

$$R_1 = 6 \Omega \quad R_2 = 3 \Omega \quad \bar{P} = 12 \text{ W}$$



$$\bar{P} = V_{\text{eff}} \cdot I_{\text{eff}} \quad \bar{P} = I_{\text{eff}}^2 \cdot R_L$$

$$I_{\text{eff}} = \sqrt{\frac{\bar{P}}{R_1}} \Rightarrow \boxed{I_{\text{eff}} = \sqrt{2} \text{ A}}$$

$$V_{\text{eff}} = I_{\text{eff}} \cdot R_1 \Rightarrow V_{\text{eff}} = 6\sqrt{2} \text{ V}$$

$$V_{\text{eff}} = \frac{V}{\sqrt{2}} \Rightarrow V = \sqrt{2} \cdot V_{\text{eff}} \Rightarrow \boxed{V = 12 \text{ Volt}}$$

Π2

$$\text{Για } \omega' = 2\omega$$

$$V' = N B A \omega' = 2V = 24 \text{ Volt}$$

$$\text{και } v = 24 \cdot \mu(1000\pi t) \text{ (S.I)}$$

$$P = v \cdot i = \frac{v^2}{R_1} \Rightarrow P = \frac{24^2 \cdot \mu^2(1000\pi t)}{6}$$

$$\Rightarrow P = 96 \cdot \mu^2(1000\pi t) \text{ (S.I)}$$

$$\text{Για } t = 5 \cdot 10^{-3} \text{ s} : P = 96 \cdot \mu^2\left(\frac{\pi}{2}\right) \Rightarrow \boxed{P = 96 \text{ W}}$$

Γ3

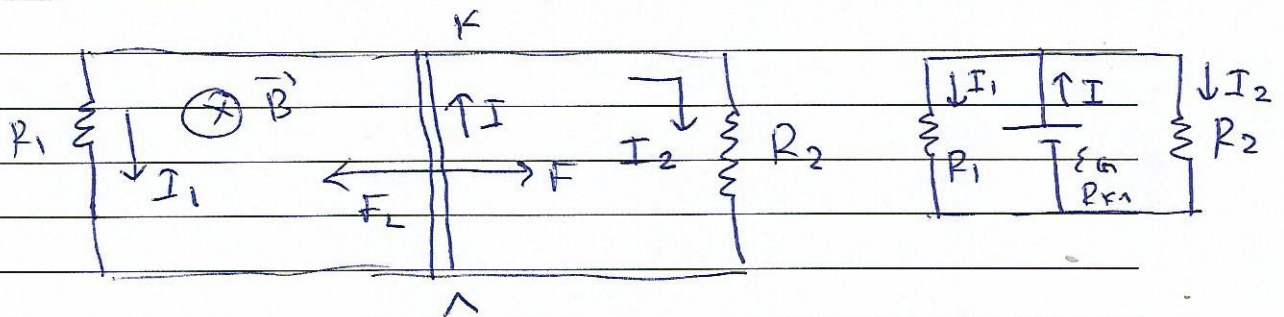
Από  $0 - t_1 = 2s$  η ράβδος εκτελεί ευθύγραμμη ομαλά επιταχυνόμενη κίνηση.

$$\text{με } a = \frac{\Sigma F}{m} = \frac{F}{m} = 1 \text{ m/s}^2$$

Άρα για  $t_1 = 2 \text{ sec}$ :  $v_1 = a \cdot t_1 \Rightarrow \boxed{v_1 = 2 \text{ m/s}}$

και  $x_1 = \frac{1}{2} a t_1^2 \Rightarrow x_1 = \frac{1}{2} \cdot 1 \cdot 2^2 \Rightarrow \boxed{x_1 = 2 \text{ m}}$

Μετά του  $t_1$  είναι  $v = 2 \text{ m/s}$



$$\Sigma F = 0 \Rightarrow F = F_L \Rightarrow F = B \cdot I \cdot l \Rightarrow$$

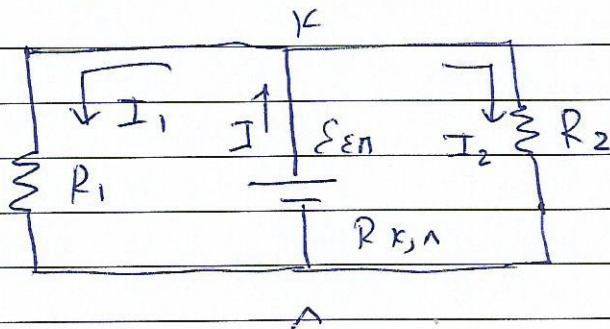
$$\Rightarrow F = \frac{B^2 v_1 \cdot l^2}{R_{02}} \Rightarrow B = \sqrt{\frac{F \cdot R_{02}}{v_1 \cdot l^2}}$$

$$R_{02} = R_{1,2} + R_{KL} = \frac{R_1 \cdot R_2}{R_1 + R_2} + R_{KL} = 4 \Omega$$

άρα  $\boxed{B = 1 \text{ T}}$

Γ4) Έχουμε πείρα σε κύκλωμα

από  $t_1 = 2 \text{ sec}$  έως  $t_2 = 5 \text{ sec}$



$$I = \frac{\varepsilon_{\text{εη}}}{R_{\text{ολ}}} = \frac{B\mu l}{R_{\text{ολ}}} = 0,5 \text{ A}$$

$$V_{\text{κλ}} = I \cdot R_{1,2} = 1,5 \text{ V} \quad (\text{ή } V_{\text{κλ}} = \varepsilon_{\text{εη}} - I \cdot R_{\text{κλ}})$$

$$I_2 = \frac{V_{\text{κλ}}}{R_2} = \frac{1}{3} \text{ A}$$

$$Q_2 = I_2^2 \cdot R_2 \cdot \Delta t = \frac{1}{9} \cdot 3 \cdot 3 = 1 \text{ J}$$

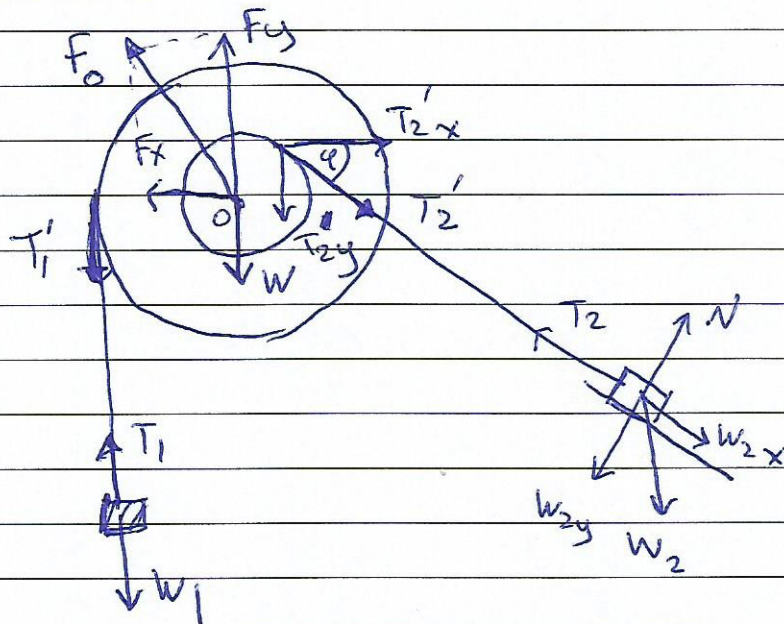
$$x_{\text{ολ}} = x_1 + x_2 = x_1 + v_1 \cdot \Delta t = 2 + 6 = 8 \text{ m}$$

$$W_F = F \cdot x_{\text{ολ}} = 4 \text{ J}$$

$$\text{άρα } \pi\% = \frac{Q}{W_F} = 25\%$$

Θέμα Δ

A1



Για το  $\Sigma_2$ :  $\Sigma F_{2x} = 0 \Rightarrow T_2 = m_2 g \mu \Rightarrow T_2 = 30 \text{ N}$

Για τροχαλία:  $\Sigma \tau = 0 \Rightarrow T_2' \cdot r - T_1' \cdot 2r = 0 \Rightarrow T_1' = 15 \text{ N}$   
(ο)

Για σώμα  $\Sigma_1$ :  $\Sigma F_y = 0 \Rightarrow W_1 = T_1 \Rightarrow \boxed{m_1 = 1,5 \text{ Kg}}$

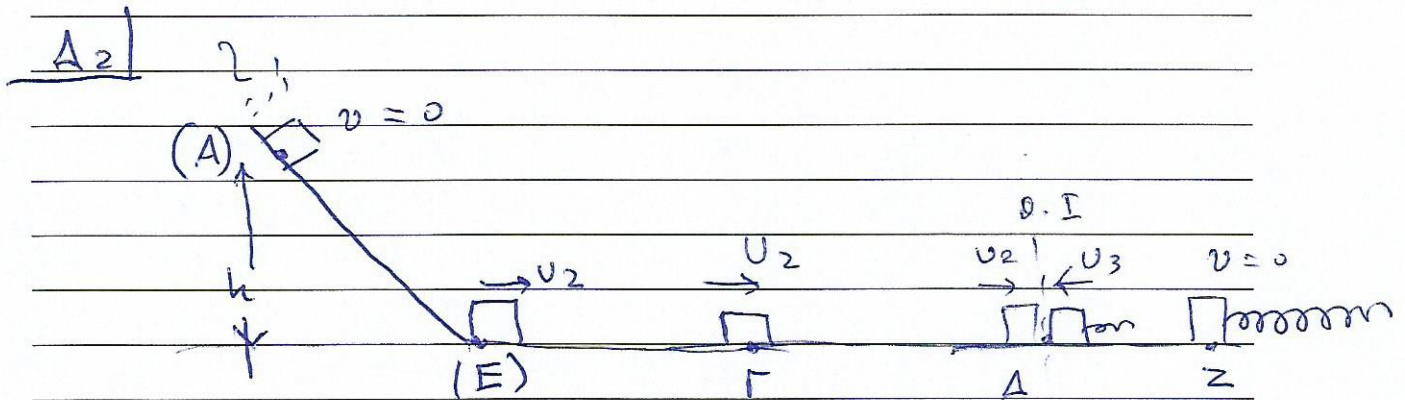
Για τροχαλία:  $\Sigma F_x = 0 \Rightarrow F_x = T_2' x \Rightarrow F_x = T_2' \cdot 0,6 \text{ m}$

$\Rightarrow F_x = 24 \text{ N}$

$\Sigma F_y = 0 \Rightarrow F_y - T_1' - W - T_2'y = 0 \Rightarrow F_y = 48 \text{ N}$

$F_0 = \sqrt{F_x^2 + F_y^2} = \sqrt{24^2 + 48^2} = 24\sqrt{5} \text{ N}$





Θ.Μ.Κ.Ε για ζ<sub>2</sub> :  $\frac{1}{2} m_2 v_2^2 - 0 = m_2 g h \Rightarrow$   
 $A \rightarrow E$   
 $\Rightarrow |v_2| = 6 \text{ m/s}$

$\Delta t_2 = \Delta t_3 \Rightarrow \frac{(\Gamma \Delta)}{|v_2|} = \frac{T}{4} \Rightarrow T = \frac{4 \cdot l}{|v_2|}$

$\Rightarrow T = 0,4 \pi \text{ sec}$  και  $\omega = \frac{2\pi}{T} = 5 \text{ rad/s}$

$D = m_3 \cdot \omega^2 \Rightarrow K = 5 \cdot 5^2 \Rightarrow \boxed{K = 125 \text{ N/m}}$

A3  $|v_3| = \omega \cdot A = \omega \cdot d \Rightarrow v_3 = \pm 1 \text{ m/s} \left( \overset{(+)}{\leftarrow} \right)$

και  $v_2 = -6 \text{ m/s}$

$m_2 = m_3$  άρα έχουμε ανταλλαγή ταχυτήτων  
 Αλλάδι

$v_2' = +1 \text{ m/s}$  και  $v_3' = -6 \text{ m/s}$

$|v_3'| = v_{\max} \Rightarrow |v_3'| = \omega \cdot A' \Rightarrow A' = 1,2 \text{ m}$

Για  $t = 0$  :  $x = 0$  και  $v_3' < 0$  ... άρα  $\varphi_0 = \pi \text{ rad}$

$$x = 1,2 \cdot \eta\mu(5t + \pi) \quad (\text{S.I})$$

Δει  $k = 8 \text{ N/m} \Rightarrow E - \text{U}_T = 8 \text{U}_T \Rightarrow E = 9 \text{U}_T$

$$\Rightarrow |x| = \frac{A'}{3} \Rightarrow |x| = 0,4 \text{ m}$$

Για 1<sup>η</sup> φορά  $x = -0,4 \text{ m}$

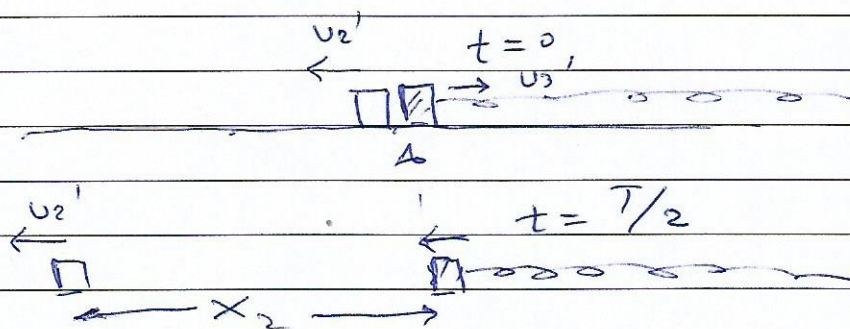
$$\frac{dP}{dt} = \Sigma F = -D \cdot x = -k \cdot x = -125 \cdot (-0,4) = +50 \text{ N} \quad \left( = \text{kg} \frac{\text{m}}{\text{s}^2} \right)$$

A.A.E 2<sup>η</sup>:  $E_T = \text{U}_T + K \Rightarrow |v| = \omega \sqrt{A'^2 - x^2} \Rightarrow$

$$\Rightarrow |v| = 5 \cdot \sqrt{1,2^2 - 0,4^2} = 5 \cdot 0,4 \cdot \sqrt{3^2 - 1^2} \Rightarrow |v| = 4\sqrt{2} \text{ m/s}$$

και  $\left| \frac{dK}{dt} \right| = |-D \cdot x \cdot v| = k \cdot |x| \cdot |v| = 200\sqrt{2} \text{ J/s}$

Α 5



$$x_2 = |v_2'| \cdot \Delta t = |v_2'| \cdot \frac{T}{2} = |v_3'| \cdot \frac{T}{2} = 1 \cdot \frac{T}{5} = \frac{T}{5} \text{ m}$$